

UNIT:4 ELECTRICITY

		FORMULAE	UNIT
1	Electric Current	$I=Q/t=\frac{\text{Charge}}{\text{time}}$	ampere (A)
2	Ohm's law	$V=IR=\text{Current} \times \text{Resistance}$ $I=V/R$ $R=V/I$	Volt Ampere Ohm (Ω)
3	Potential difference	$V=W/Q=\frac{\text{workdone}}{\text{charge}}$	Volt (V)
4	Resistivity	$\rho = RA/L$	Ohm-metre (Ωm)
5	Conductance	$G=1/R$	Ohm ⁻¹ (mho)
6	Conductivity	$\sigma = \frac{1}{\rho}$	Ohm ⁻¹ meter-1 (mhom ⁻¹)
7	Equivalent resistance in a series combination	$R_s=R_1R_2+R_3$ (or) $R_s=nR$	
8	Equivalent resistance in a parallel combination	$\frac{1}{R_p}=\frac{1}{R_1}+\frac{1}{R_2}+\frac{1}{R_3}$	
9	Electric Power	$P=\frac{\text{work}}{\text{time}}=\frac{VIt}{t}$ (or) $P=VI$	watt (W)
10	Joule's law of Heating	$H=VIt$ $H=I^2Rt$ ($\therefore V=IR$)	Joule (J)

VI. Very short answer questions: Pg.No.56

2. What happens to the resistance, as the conductor is made thicker?

Ans: i) The resistance decreases as the conductor is made thicker.

Reason: Resistance is inversely proportional to area of cross section A. $R \propto \frac{1}{A}$

3. Why is tungsten metal used in bulbs, but not in fuse wires?

Ans: Tungsten has high melting point, it can bear high heat for glowing. But it is not used in fuse wires, because a metal (wire) which has low melting point should be used in a fuse wire.

IX. Numerical Problems: (Pg.No.57)

1. An electric iron consumes energy at the rate of 420 W when heating is at the maximum rate and 180 W when heating is at the minimum rate. The applied voltage is 220V. What is the current in each case?

Ans: i) When heating is maximum:

$$P_1 = 420 \text{ W}$$

Applied Voltage (V) = 220V

$$P=VI$$

Current I = P/V

$$I = \frac{420}{220} = 1.909\text{A}$$

$$I=1.909\text{A}$$

ii) When heating is minimum:

$$P_2=180\text{W}$$

Applied voltage V=220V

$$P=VI$$

$$I=P/V$$

$$I=\frac{180}{220} = 0.818\text{A}$$

$$I=0.818\text{A}$$

2. A 100 watt electric bulb is used for 5 hours daily and four 60 watt bulbs are used for 5 hours daily. Calculate the energy consumed (in KWh) in the month of January.

Ans: Energy used by 100W bulb is $E=P \times t$

$$=100 \times 5$$

$$=500\text{Wh}$$

Energy used by four 60W bulbs $E=4 \times 60 \times 5$

$$=1200\text{Wh}$$

Total energy per day = 500 + 1200

$$= 1700 \text{ Wh}$$

$$= 1.7 \text{ KWh}$$

Number of days in January = 31days

Energy consumed in January = 31 \times 1.7

$$= 52.7 \text{ KWh}$$

3. A torch bulb is rated at 3V and 600mA, calculate it's

a) Power

b) resistance

c) energy consumed if it is used for 4 hour.

Ans: a) $P=VI$

$$P= 3 \times 0.6 = 1.8\text{W}$$

b) $V=IR$

$$R= \frac{V}{I} = \frac{3}{0.6} = 5\Omega$$

c) Energy consumed for 4 hours

$$= \text{Power of the bulb} \times \text{time}$$

$$= 1.8W \times 4h$$

$$= 7.2 Wh$$

4. A piece of wire having a resistance R is cut into five equal parts.

- How will the resistance of each part of the wire change compared with the original resistance?
- If the five parts of the wire are placed in parallel, how will the resistance of the combination change?
- What will be the ratio of the effective resistance in series connection to that of the parallel connection?

Solution: a) Resistance of a piece of wire is proportional to its length.

$$R \propto L$$

Each piece has a resistance = R

Wire is cut into five equal parts

Resistance of each part = $R/5$

b) All the five parts are connected in parallel, the effective resistance is

$$\frac{1}{R_p} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$$

$$\frac{1}{R_p} = \frac{5}{R} + \frac{5}{R} + \frac{5}{R} + \frac{5}{R} + \frac{5}{R}$$

$$\frac{1}{R_p} = \frac{25}{R}$$

$$\therefore R_p = \frac{R}{25}$$

c) The ratio of the effective resistance in series to parallel connection.

$$\frac{1}{R_p} = \frac{25}{R_s}$$

$$\frac{R_s}{R_p} = \frac{25}{1}$$

Ratio of R_s & R_p = 25:1

$R_s : R_p = 25 : 1$

X. Hot Questions:

- Two resistors when connected in parallel give the resultant resistance of 2 Ohm; but when connected in series the effective resistance becomes 9 Ohm. Calculate the value of each resistance.

Solution: Effective resistance in parallel $R_p = 2\Omega$

Effective resistance in series $R_s = 9\Omega$

$$R_s = R_1 + R_2$$

$$\frac{1}{R_p} = \frac{1}{R_1} + \frac{1}{R_2}$$

$$R_s = R_1 + R_2 = 9$$

$$R_2 = 9 - R_1$$

$$\frac{1}{R_1} + \frac{1}{R_2} = \frac{1}{R_p} = \frac{1}{2}$$

$$\frac{1}{R_1} + \frac{1}{9 - R_1} = \frac{1}{2}$$

$$\frac{9 - R_1 + R_1}{R_1(9 - R_1)} = \frac{9}{9R_1 - R_1^2}$$

$$\frac{9}{9R_1 - R_1^2} = 1/2$$

$$9R_1 - R_1^2 = 18$$

$$-R_1^2 + 9R_1 = 18 = 0$$

$$-R_1^2 - 9R_1 + 18 = 0$$

$$(R_1 - 3)(R_1 - 6) = 0$$

$$\therefore R_1 = 3, 6$$

When $R_1 = 3\Omega$, $R_2 = 9 - 3 = 6\Omega$

When $R_1 = 6\Omega$, $R_2 = 9 - 6 = 3\Omega$

- How many electrons are passing per second in a circuit in which there is a current of 5A?

Solution: $I = Q/t$

Where charge of electron which is equal to $1.6 \times 10^{-19}c$

'Q' no. of charges ($Q = ne$)

$$I = \frac{ne}{t} \quad (t = IS)$$

$$n = \frac{It}{e} = \frac{5 \times 1}{1.6 \times 10^{-19}}$$

Number of electrons

$$n = 3.125 \times 10^{19} \text{ electrons}$$

- A piece of wire of resistance 10 ohm is drawn out so that its length is increased to three times its original length. Calculate the new resistance.

Solution: $R = 10 \text{ Ohm}$; Length is increased thrice = $3L$

$$R = \frac{\rho L}{A}$$

$$10 = \frac{\rho L}{A}$$

When the length is increased by three times ($3L$) the area of cross section is reduced by three times. ($A/3$)

New length = $3L$

New Area = $A/3$

$$\therefore \text{New Resistance } R = \frac{\rho \times 3L}{\frac{A}{3}} = 9 \left(\frac{\rho L}{A} \right)$$

$$R = 9 \times R$$

$$= 9 \times 10$$

$$R = 90 \Omega$$